

$$Y_{cg} := \frac{510 \cdot 810 \cdot \frac{810}{2} + 2 \cdot \left( 300 \cdot 150 \cdot \frac{300}{2} \right)}{810 \cdot 510 + 2 \cdot 300 \cdot 150}$$

$$Y_{cg} := \text{round}(Y_{cg}, 0) \text{ mm}$$

$$Y_{cg} = 359 \text{ mm}$$

$$c2 := 359 \text{ mm}$$

$$c1 := 810 \text{ mm} - c2$$

$$x := 510 \cdot \frac{810^3}{12} \text{ mm}^4 + 510 \cdot 810 \cdot \left( \frac{810 \text{ mm}}{2} - c2 \right)^2 \text{ mm}^2$$

$$y := 2 \cdot \left[ 150 \cdot \frac{300^3}{12} \text{ mm}^4 + 150 \cdot 300 \text{ mm}^2 \cdot \left( \frac{300 \text{ mm}}{2} - c2 \right)^2 \right]$$

$$I := x + y$$

$$I = 2.807 \times 10^{10} \text{ mm}^4$$

$$A_c := 510 \cdot 810 \text{ mm}^2 + 2 \cdot 300 \cdot 150 \text{ mm}^2$$

$$S2 := \frac{I}{c2} \quad r := \sqrt{\frac{I}{A_c}}$$

## Datos

$$P_i := 3250 \text{ kN}$$

$$R := 0.8$$

$$e := 285 \text{ mm}$$

$$f_c := 35 \text{ MPa}$$

$$f_{ci} := 30 \text{ MPa}$$

$$A_p := 2700 \text{ mm}^2$$

$$\varepsilon_{cu} := 0.002$$

$$b := 510 \text{ mm}$$

$$d_p := 735 \text{ mm}$$

## 1.- Cálculos

$$P_e := P_i \cdot R$$

$$f_r := 0.625 \sqrt{\frac{f_c}{1 \text{ MPa}}} \cdot \text{MPa}$$

$$M_{cr} := f_r \cdot S2 + P_e \cdot \left( \frac{r^2}{c2} + e \right)$$

$$P_e = 2.6 \times 10^3 \text{ kN}$$

$$c2 = 359 \text{ mm}$$

$$S2 = 7.818 \times 10^7 \text{ mm}^3$$

$$f_r = 3.698 \text{ MPa}$$

$$r^2 = 5.579 \times 10^4 \text{ mm}^2$$

$$M_{cr} = 1.434 \times 10^3 \text{ kN} \cdot \text{m}$$

## 2a.- Cálculos

$$E_p := 1500 \frac{\text{MPa}}{0.008} \quad E_c := 4700 \sqrt{\frac{f_c}{1 \text{MPa}}} \text{MPa} \quad \varepsilon_1 := \frac{P_e}{A_p \cdot E_p} \quad \varepsilon_2 := \frac{P_e}{A_c \cdot E_c} \cdot \left( 1 + \frac{e^2}{r^2} \right)$$

$$\beta_1 := 0.85 - 0.008 \left( \frac{f_c}{1 \text{MPa}} - 30 \right) \quad f_{pu} := 1800 \text{MPa} \quad f_{py} := 1500 \text{MPa}$$

*Tomo fps por Iteración*

$$fps := 1505 \text{MPa}$$

$$a := A_p \cdot \frac{fps}{\beta_1 \cdot f_c \cdot b} \quad c := \frac{a}{\beta_1} \quad \varepsilon_3 := \varepsilon_{cu} \cdot \frac{d_p - c}{c} \quad \varepsilon_s := \varepsilon_1 + \varepsilon_2 + \varepsilon_3$$

$$\text{resp} := \text{if}(a \leq 510 \text{mm}, \text{"Viga Rectangular"}, \text{"Viga T"}) \quad \text{resp} = \text{"Viga Rectangular"}$$

$$\varepsilon_1 = 5.136 \times 10^{-3} \quad \varepsilon_2 = 4.565 \times 10^{-4} \quad \varepsilon_3 = 3.355 \times 10^{-3} \quad \varepsilon_s = 8.947 \times 10^{-3}$$

$$a = 281.046 \text{mm} \quad c = 346.97 \text{mm} \quad \beta_1 = 0.81$$

$$fps := \text{if} \left[ \varepsilon_s \leq 0.008, \frac{1500}{0.008} \cdot \varepsilon_s, \frac{f_{pu} - f_{py}}{(0.067 - 0.008) \cdot 1 \text{MPa}} \cdot (\varepsilon_s - 0.008) + 1500 \right] \cdot \text{MPa}$$

$$M_n := A_p \cdot fps \cdot \left( d_p - \frac{a}{2} \right)$$

$$fps = 1.505 \times 10^3 \text{MPa}$$

$$M_n = 2.415 \times 10^3 \text{kN}\cdot\text{m}$$

## 2b.- Cálculos

*Según ACI*

$$\rho_p := \frac{A_p}{b \cdot d_p} \quad \frac{f_{py}}{f_{pu}} = 0.833$$

$$\gamma_p := \text{if} \left[ \left( 0.8 \leq \frac{f_{py}}{f_{pu}} \right) < 0.85, 0.55, \text{if} \left( 0.85 \leq \frac{f_{py}}{f_{pu}} < 0.9, 0.4, 0.28 \right) \right] \quad \gamma_p = 0.55$$

$$f_{ps} := f_{pu} \cdot \left( 1 - \frac{\gamma_p}{\beta_1} \cdot \rho_p \cdot \frac{f_{pu}}{f_c} \right) \quad f_{ps} = 1.347 \times 10^3 \text{ MPa}$$

$$M_n := A_p \cdot f_{ps} \cdot \left( d_p - \frac{a}{2} \right) \quad M_n = 2.162 \times 10^3 \text{ kN}\cdot\text{m}$$

*y con  $\gamma_p$  de 0.4, para los que no consideraron el 1er caso*

$$\gamma_p := 0.4$$

$$f_{ps} := f_{pu} \cdot \left( 1 - \frac{\gamma_p}{\beta_1} \cdot \rho_p \cdot \frac{f_{pu}}{f_c} \right) \quad f_{ps} = 1.471 \times 10^3 \text{ MPa}$$

$$M_n := A_p \cdot f_{ps} \cdot \left( d_p - \frac{a}{2} \right) \quad M_n = 2.361 \times 10^3 \text{ kN}\cdot\text{m}$$