

MA34B - Estadística - Tabla de Distribuciones

| Distribución | Sigla | Densidad | E(X) | Var(X) | f.g.m. |
|-------------------|-------------------------|--|-------------------------------|--|--|
| Bernoulli | Ber(p) | $p^k (1-p)^{1-k}$ $k=0,1 \quad 0 \leq p \leq 1$ | p | p(1-p) | $(pe^t + 1-p)$ |
| Binomial | B(n,p) | $\binom{n}{z} p^z (1-p)^{n-z}$ $z=0, \dots, n \quad 0 \leq p \leq 1$ | np | np(1-p) | $(pe^t + 1-p)^n$ |
| Binomial Negativa | BN(r,p) | $\binom{r-1}{z-1} p^{z-1} (1-p)^{n-z}$ $z=1, \dots, n \quad 0 \leq p \leq 1$ | $\frac{r(1-p)}{p}$ | $\frac{r(1-p)}{p^2}$ | $\left(\frac{pe^t}{1-(1-p)e^t} \right)^r$ |
| Beta | Beta(α, β) | $\frac{\Gamma(\alpha+\beta)}{\Gamma(\alpha)\Gamma(\beta)} x^{\alpha-1} (1-x)^{\beta-1}$ $0 < x < 1 \quad \alpha > 0, \beta > 0$ | $\frac{\alpha}{\alpha+\beta}$ | $\frac{\alpha\beta}{(\alpha+\beta)^2(\alpha+\beta)}$ | |
| Poisson | P(λ) | $\frac{\lambda^k e^{-\lambda}}{k!}$ $k=0, \dots, \infty \quad \lambda > 0$ | λ | λ | $e^{\lambda(e^t-1)}$ |
| Uniforme | U(a,b) | $\frac{1}{b-a} \quad a \leq x \leq b$ | $\frac{a+b}{2}$ | $\frac{(b-a)^2}{12}$ | $\frac{e^{bt} - e^{at}}{(b-a)t}$ |

| | | | | | |
|--------------|-----------------------|---|------------------------|---------------------------------|---|
| Gamma | $G(\alpha, \beta)$ | $\frac{\beta^\alpha}{\Gamma(\alpha)} x^{\alpha-1} e^{-\beta x}$ $x > 0 \quad \alpha > 0, \beta > 0$ | $\frac{\alpha}{\beta}$ | $\frac{\alpha}{\beta^2}$ | $\left(\frac{\beta}{\beta-t}\right)^\alpha$ |
| Exponencial | $\text{Exp}(\lambda)$ | $\lambda e^{-\lambda x} \quad x > 0, \lambda > 0$ | $\frac{1}{\lambda}$ | $\frac{1}{\lambda^2}$ | $\frac{\lambda}{\lambda-t}$ |
| Chi Cuadrado | χ_n^2 | $\frac{x^{\frac{n}{2}-1} e^{-\frac{x}{2}}}{2^{\frac{n}{2}} \Gamma\left(\frac{n}{2}\right)} \quad x \geq 0$ | n | 2n | $\frac{1}{(1-2t)^{n/2}}$ |
| Normal | $N(\mu, \sigma^2)$ | $\frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{1}{2}\frac{(x-\mu)^2}{\sigma^2}}$ $-\infty \leq x \leq \infty$ | μ | σ^2 | $e^{t\mu + \frac{\sigma^2 t^2}{2}}$ |
| t- Student | t_n | $\frac{\Gamma\left(\frac{n+1}{2}\right)}{(n\pi)^{\frac{1}{2}} \Gamma\left(\frac{n}{2}\right)} \left(1 + \frac{x^2}{n}\right)^{-\frac{(n+1)}{2}}$ $-\infty \leq x \leq \infty$ | 0 para $n > 1$ | $\frac{n}{n-2}$ para $n > 2$ | |
| F- Fisher | $F_{m,n}$ | $\frac{\Gamma\left(\frac{1}{2}(m+n)\right) m^{\frac{m}{2}} n^{\frac{n}{2}}}{\Gamma\left(\frac{1}{2}m\right) \Gamma\left(\frac{1}{2}n\right)} \frac{x^{\frac{m}{2}-1}}{(mx+n)^{\frac{m+n}{2}}}$ $x > 0$ | | | |

OBS: $\Gamma(p) = \int_0^\infty x^{p-1} e^{-x} dx$ y $\Gamma(p) = (p-1)\Gamma(p-1)$