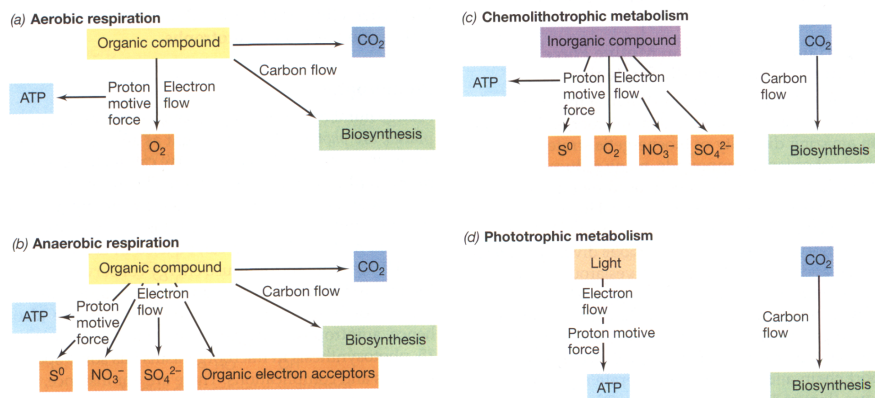


# Tema 3 – Bioenergía Bioenergetics

CI7115 – Biotecnología Ambiental  
Prof. Ana Lucía Prieto Santa



## Relaciones energéticas y flujo de carbono




Brock, 2000

Acetate and carbon dioxide (methanogenesis of acetate)		$\Delta G^\circ$ , kJ
Donor:	$\frac{1}{8}\text{CH}_3\text{COO}^- + \frac{3}{8}\text{H}_2\text{O} = \frac{1}{8}\text{CO}_2 + \frac{1}{8}\text{HCO}_3^- + \text{H}^+ + \text{e}^-$	-27.40
Acceptor:	$\frac{1}{8}\text{CO}_2 + \text{H}^+ + \text{e}^- = \frac{1}{8}\text{CH}_4 + \frac{1}{4}\text{H}_2\text{O}$	23.53
Net:	$\frac{1}{8}\text{CH}_3\text{COO}^- + \frac{1}{8}\text{H}_2\text{O} = \frac{1}{8}\text{CH}_4 + \frac{1}{8}\text{HCO}_3^-$	-3.87
Glucose and carbon dioxide (methanogenesis from glucose)		$\Delta G^\circ$ , kJ
Donor:	$\frac{1}{24}\text{C}_6\text{H}_{12}\text{O}_6 + \frac{1}{4}\text{H}_2\text{O} = \frac{1}{4}\text{CO}_2 + \text{H}^+ + \text{e}^-$	-41.35
Acceptor:	$\frac{1}{8}\text{CO}_2 + \text{H}^+ + \text{e}^- = \frac{1}{8}\text{CH}_4 + \frac{1}{4}\text{H}_2\text{O}$	23.53
Net:	$\frac{1}{24}\text{C}_6\text{H}_{12}\text{O}_6 = \frac{1}{8}\text{CH}_4 + \frac{1}{8}\text{CO}_2$	-17.82
Hydrogen and oxygen (aerobic oxidation of hydrogen)		$\Delta G^\circ$ , kJ
Donor:	$\frac{1}{2}\text{H}_2 = \text{H}^+ + \text{e}^-$	-39.87
Acceptor:	$\frac{1}{4}\text{O}_2 + \text{H}^+ + \text{e}^- = \frac{1}{2}\text{H}_2\text{O}$	-78.72
Net:	$\frac{1}{2}\text{H}_2 + \frac{1}{4}\text{O}_2 = \frac{1}{2}\text{H}_2\text{O}$	-118.59

**Basic concepts in bioenergy:**

- Oxidation number (state)
- Gibbs Free Energy
- Acid-base chemistry

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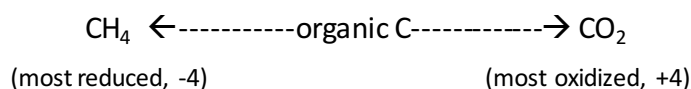
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## Cálculo de número o estado de oxidación

1. The oxidation state of an element in an elementary substance is zero (ex.  $\text{H}_2, \text{O}_2, \text{Fe}^0$ )
2. The oxidation state of the ion of an element is equal to its charge  
 $\text{Na}^+ = +1, \text{Fe}^{3+} = +3$
3. The sum of oxidation numbers of all atoms in a neutral molecule is zero.  
Thus,  $\text{H}_2\text{O}$  is neutral because it has two H at +1 each and one O at -2.
4. In an ion, the sum of oxidation numbers of all atoms is equal to the charge on that ion. Thus, in the  $\text{OH}^-$  ion,  $\text{O}(-2) + \text{H}(+1) = -1$ .
5. In compounds, the oxidation state of O is virtually always -2, and that of H is +1.

## Cálculo de número o estado de oxidación

6. In simple carbon compounds, the oxidation state of C can be calculated by adding up the H and O atoms present and using the oxidation states of these elements as given in item 5, because in a neutral compound the sum of all oxidation number must be zero. Thus, the oxidation state of carbon in methane (CH<sub>4</sub>) is -4 (4 H at +1 each = +4); in carbon dioxide (CO<sub>2</sub>), the oxidation state of carbon is +4 (2 O at -2 each = -4).



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## Cálculo de número o estado de oxidación

7. In organic compounds with more than one C atom, it may not be possible to assign a specific oxidation number to each C atom, but it is still useful to calculate the oxidation state of the compound as a whole. The same conventions are used.

Thus, the oxidation state of carbon in glucose (C<sub>6</sub>H<sub>12</sub>O<sub>6</sub>) is zero (12 H at +1 = 12; 6 O at -2 = -12) and the oxidation state of carbon in ethanol (C<sub>2</sub>H<sub>5</sub>OH) is -2 each (6 H at +1 = +6; one O at -2).



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## Cálculo de número o estado de oxidación

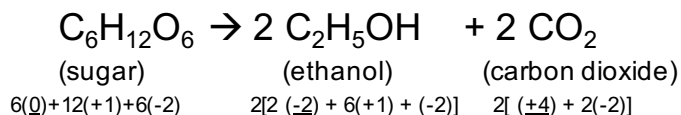
8. In all oxidation-reduction reactions there is a balance between the oxidized and reduced products. To calculate an oxidation-reduction balance, the number of molecules of each product is multiplied by its oxidation state. For instance, in calculating the oxidation-reduction balance for alcohol fermentation, there are two molecules of ethanol at  $-4 = -8$  and two molecules of  $\text{CO}_2$  at  $+4 = +8$  so the net balance is zero. When constructing model reactions, it is useful to calculate redox balances to be certain that the reaction is possible (**electroneutrality** must be maintained).



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## Ejemplo: Fermentación del Alcohol



4 carbons were reduced      2 carbons were oxidized  
to  $-2 = -8$  overall              to  $+4 = +8$  overall



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## Ciclo del N y especiación

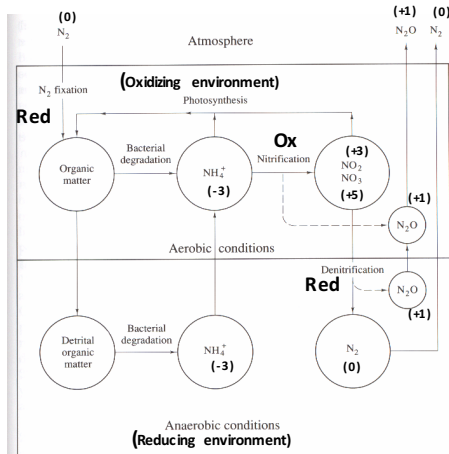


Figure 12.1 Microbial transformations of nitrogen in the global cycle. From Wollast (1981).

Ox = oxidation reaction, electron acceptor (e.g., O<sub>2</sub>) needed  
 Red = reduction reaction, electron donor (e.g., H<sub>2</sub>) needed



Schlesinger, 1991, Biogeochemistry: Analysis of Global Change.

Table 15.3. Summary of the Principal Oxidation-Reduction Chemistry of Nitrogen

Oxidation State	Species	Remarks
+5	NO <sub>3</sub> <sup>-</sup>	Nitrate ion, a strong oxidizing agent in acid solution.
+4	NO <sub>2</sub> N <sub>2</sub> O <sub>4</sub>	Nitrogen dioxide, a red-brown gas; the chief reduction product of concentrated nitric acid. Nitrogen dioxide dimerizes to form dinitrogen tetroxide, N <sub>2</sub> O <sub>4</sub> .
+3	NO <sub>2</sub> <sup>-</sup> HNO <sub>2</sub>	Nitrite ion, in basic solution. Nitrous acid, in acid solution. Both can act either as an oxidizing agent or as a reducing agent. When acting as a reducing agent, they are oxidized to NO <sub>3</sub> <sup>-</sup> . When HNO <sub>2</sub> acts as an oxidizing agent in acid solution it is usually reduced to NO(g).
+2	NO	Nitrogen oxide (nitric oxide), a colorless gas; the chief reduction product of dilute nitric acid.
+1	N <sub>2</sub> O	Dinitrogen oxide (nitrous oxide), also called laughing gas. Not usually formed in oxidation-reduction reactions in aqueous solution.
0	N <sub>2</sub>	Unreactive because of the strong triple bond, $\text{N}\equiv\text{N}$ .
-1	NH <sub>2</sub> OH	Hydroxylamine, a weak base. Can serve both as an oxidizing agent and as a reducing agent.
-2	N <sub>2</sub> H <sub>4</sub>	Hydrazine, a colorless liquid that disproportionates to N <sub>2</sub> and NH <sub>3</sub> . Hydrazine is a weak base.
-3	NH <sub>3</sub> NH <sub>4</sub> <sup>+</sup>	In basic solution. In acidic solution. Rarely used as a reducing agent in aqueous solution. When ammonia is burned in O <sub>2</sub> it is oxidized to either N <sub>2</sub> or NO depending on conditions. Oxidation of ammonium salts generally produces N <sub>2</sub> .

Segal, Chemistry: experiment and theory. 1985

## Especiación del Cloro

Table 15.4. Summary of the Principal Oxidation-Reduction Chemistry of Chlorine

Oxidation State	Species	Remarks
+7	ClO <sub>4</sub> <sup>-</sup>	Perchlorate ion, a powerful oxidizing agent.
+5	ClO <sub>3</sub> <sup>-</sup>	Chlorate ion, a powerful oxidizing agent.
+4	ClO <sub>2</sub>	Chlorine dioxide, a yellow-orange gas. Not a common oxidation state of chlorine, but it is formed when ClO <sub>3</sub> <sup>-</sup> reacts with a number of reducing agents. Chlorine dioxide can serve as an oxidizing agent also.
+3	ClO <sub>2</sub> <sup>-</sup>	Chlorite ion, in basic solution. Serves as an oxidizing agent in bleaches. In acid solution HClO <sub>2</sub> disproportionates to ClO <sub>2</sub> (g) and Cl <sup>-</sup> .
+1	ClO <sup>-</sup> HOCl	Hypochlorite ion, in basic solution. Hypochlorous acid, in acid solution. Both serve as oxidizing agents. ClO <sup>-</sup> disproportionates when warmed, to yield Cl <sup>-</sup> and ClO <sub>3</sub> <sup>-</sup> .
0	Cl <sub>2</sub>	Chlorine, a good oxidizing agent.
-1	Cl <sup>-</sup>	Chloride ion, a moderately good reducing agent.

Segal, Chemistry: experiment and theory. 1985

• Note:

- Perchlorate (used in rocket fuels and now contaminating groundwater) is already highly oxidized, cannot be destroyed by oxidation; need to be reduced (electron donors, e.g., H<sub>2</sub> needed)

Chloride ion is a reduced species. Thus, the reductive dechlorination process, in which chlorine is sequentially removed as chloride from a chlorinated organic compound (e.g. PCB) involves electron donors.



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## Energía libre de Gibb's

1.  $\Delta G^0$  = **standard free-energy change** of the reaction at 1 atm pressure and 1 M concentrations

$\Delta G^{0r}$  = free-energy change under standard conditions at pH 7

$\Delta G$  = free-energy change under the conditions specified.

2. Calculation of  $\Delta G^0$  for a chemical reaction from the **free energy of formation,  $G_f^0$** , of products and reactants:

$$\Delta G^0 = \sum \Delta G_f^0(\text{products}) - \sum \Delta G_f^0(\text{reactants})$$

That is, sum the  $\Delta G_f^0$  of products, sum the  $\Delta G_f^0$  of reactants, and subtract the latter from the former.

Value of  $\Delta G$ :

- if negative, reaction is energy yielding and will proceed favorably (**exergonic**)

- if positive, reaction is energy consuming and will not proceed favorably

(**endergonic**)



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(Brock, Appendix A)

## Energía libre de Gibb's

3. For energy-yielding reactions involving  $H^+$ , converting from standard conditions (pH 0) to cellular conditions (pH 7):

$$\Delta G^{0r} = \Delta G^0 + m \Delta G_f^0(H^+)$$

(@pH 7)    (@pH 0)    (-39.83)

where  $m$  is the net number of protons in the reaction ( $m$  is negative when more protons are consumed than formed) and  $\Delta G_f^0(H^+)$  is the free energy of formation of a proton at pH 7 (-39.83 kJ) at 25°C.



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## Energía libre de Gibb's

- 4. Effect of concentrations on  $\Delta G$ :** With soluble substrates, the concentration ratios of products formed to exogenous substrates used are generally equal to or greater than  $10^{-2}$  at the beginning of growth and equal to or less than  $10^{-2}$  at the end of growth. From the relation between  $\Delta G$  and the equilibrium constant (see item 8), it can be calculated that  $\Delta G$  for the free-energy yield in practical situations differs from the free-energy yield under standard conditions by at most 11.7 kJ, a rather small amount, and so for a first approximation, standard free-energy yields can be used in most situations.

However, with  $H_2$  as a product,  $H_2$ -consuming bacteria present may keep the concentration of  $H_2$  so low that the free-energy yield is significantly affected. Thus, in the fermentation of ethanol to acetate and  $H_2$  by syntrophic bacteria ( $C_2H_5OH + H_2O \rightarrow C_2H_3O_2^- + 2H_2 + H^+$ ), the  $\Delta G^{0'}$  at 1 atm  $H_2$  is +9.68 kJ, but at  $10^{-4}$  atm  $H_2$  it is -36.03 kJ. With  $H_2$ -consuming bacteria present, therefore, the ethanol fermentation becomes **exergonic**. (See also item 9.)

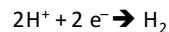


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## Energía libre de Gibb's

**5. Reduction potentials:** by convention, electrode equations are written in the direction, **oxidant +  $ne^- \rightarrow$  reductant** (that is, as reductions), where  $n$  is the number of electrons transferred. The standard potential ( $E_0'$ ) of the hydrogen electrode,



is set by definition at 0.0 V at 1 atm pressure of  $H_2$  gas and 1.0 M  $H^+$ , at 25°C.  $E_0'$  is the standard reduction potential at pH 7.

**6. Relation of free energy to reduction potential:**

$$\Delta G^{0'} = -nF\Delta E_0'$$

where  $n$  is the number of electrons transferred,  $F$  is the **Faraday constant** (96.48 kJ/V), and  $\Delta E_0'$  is the  $E_0'$  of the electron-*accepting* couple minus the  $E_0'$  of the electron-*donating* couple.



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## Energía libre de Gibb's



7. **Equilibrium constant,  $K$ .** For the generalized reaction

$$K = \frac{[C]^c [D]^d}{[A]^a [B]^b}$$

where A, B, C, and D represent reactants and products;  $a$ ,  $b$ ,  $c$ , and  $d$  represent number of molecules of each; and brackets indicate concentrations. This is true only when the chemical system is in equilibrium.

8. **Relation of equilibrium constant  $K$  to free-energy change.** At constant temperature, pressure, and pH:

$$\Delta G = \Delta G^{0'} + RT \ln K \quad (\text{for actual condition})$$

where  $R$  is a constant (**8.29 J/mol/°K**) and  $T$  is the absolute temperature (in °K).



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## Energía libre de Gibb's

9. **Two substances can react in a redox reaction even if the standard potentials are unfavorable, provided that the concentrations are appropriate.**

Assume that normally the reduced form of A would donate electrons to the oxidized form of B. However, if the concentration of the reduced form of A was low and the concentration of the reduced form of B was high, it would be possible for the reduced form of B to donate electrons to the oxidized form of A. Thus, the reaction would proceed in the direction opposite that predicted from standard potentials.

A practical example of this is the utilization of  $H^+$  as an electron acceptor to produce  $H_2$ . Normally,  $H_2$  production in fermentative bacteria is not extensive because  $H^+$  is a poor electron acceptor; the  $E_0'$  of the  $2 H^+/H_2$  pair is  $-0.41$  V. However, if the concentration of  $H_2$  is kept low by continually removing it (a process done by methanogenic prokaryotes, which use  $H_2 + CO_2$  to produce methane,  $CH_4$ , or by many other anaerobes capable of consuming  $H_2$  anaerobically), the potential will be more positive and then  $H^+$  will be a suitable electron acceptor (to produce  $H_2$ ).

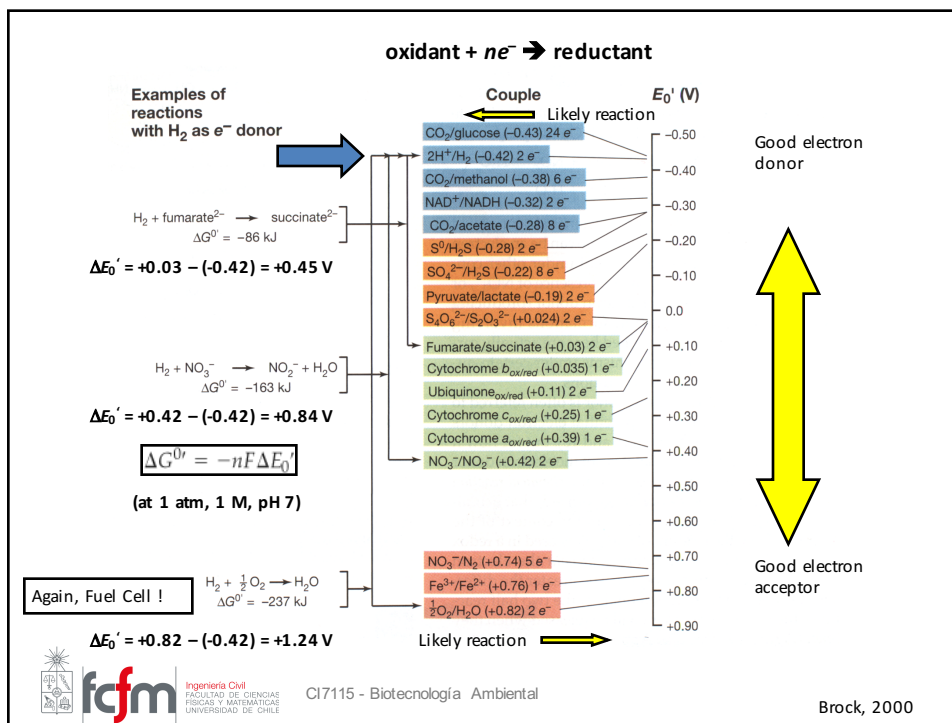


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(Brock, Appendix A)





## Combustibles (Donadores de e<sup>-</sup>)

Organic molecules are good fuels. For CO<sub>2</sub>/organic molecule couples, E<sup>o</sup> < 0 (so they are > 0 when the organic is oxidized to CO<sub>2</sub>). When coupled to reduction half reactions for oxidants, the resulting whole reactions have positive voltages E > 0.

Some inorganics are also good fuels:

best	e <sup>-</sup> donor	Half reaction	E <sup>o</sup> (V)
	HSO <sub>3</sub> <sup>-</sup>	SO <sub>4</sub> <sup>2-</sup> + 3H <sup>+</sup> + 2e <sup>-</sup> = HSO <sub>3</sub> <sup>-</sup> + H <sub>2</sub> O	-0.51
	H <sub>2</sub>	2H <sup>+</sup> + 2e <sup>-</sup> = H <sub>2</sub>	-0.41
	S <sub>2</sub> O <sub>3</sub> <sup>2-</sup>	2SO <sub>4</sub> <sup>2-</sup> + 10H <sup>+</sup> + 8e <sup>-</sup> = S <sub>2</sub> O <sub>3</sub> <sup>2-</sup> + 5H <sub>2</sub> O	-0.25
	HS <sup>-</sup>	SO <sub>4</sub> <sup>2-</sup> + 9H <sup>+</sup> + 8e <sup>-</sup> = HS <sup>-</sup> + 4H <sub>2</sub> O	-0.22
	S	SO <sub>4</sub> <sup>2-</sup> + 8H <sup>+</sup> + 6e <sup>-</sup> = S + 4H <sub>2</sub> O	-0.20
	AsO <sub>3</sub> <sup>3-</sup>	AsO <sub>4</sub> <sup>3-</sup> + 4H <sup>+</sup> + 2e <sup>-</sup> = H <sub>2</sub> AsO <sub>3</sub> <sup>-</sup> + H <sub>2</sub> O	+0.15
	Cu <sup>+</sup>	Cu <sup>2+</sup> + e <sup>-</sup> = Cu <sup>+</sup>	+0.16
	Se	SeO <sub>4</sub> <sup>2-</sup> + 8H <sup>+</sup> + 6e <sup>-</sup> = Se + 4H <sub>2</sub> O	+0.33
	NH <sub>4</sub> <sup>+</sup>	NO <sub>3</sub> <sup>-</sup> + 10H <sup>+</sup> + 8e <sup>-</sup> = NH <sub>4</sub> <sup>+</sup> + 3H <sub>2</sub> O	+0.36
	Mn (II)	MnO <sub>2</sub> + 4H <sup>+</sup> + 2e <sup>-</sup> = Mn <sup>2+</sup> + 2H <sub>2</sub> O	+0.47
worst	Fe (II)	Fe <sup>3+</sup> + e <sup>-</sup> = Fe <sup>2+</sup>	+0.77

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## Oxidantes (receptores de e<sup>-</sup>)

e <sup>-</sup> acceptor	Half reaction	E <sup>o</sup> (V)
N <sub>2</sub> O	$N_2O + 2H^+ + 2e^- = N_2 + H_2O$	+1.31
ClO <sub>3</sub> <sup>-</sup>	$ClO_3^- + 6H^+ + 6e^- = Cl^- + 3H_2O$	+1.04
NO <sub>2</sub> <sup>-</sup>	$2NO_2^- + 8H^+ + 6e^- = N_2 + 4H_2O$	+0.94
O <sub>2</sub>	$O_2 + 4H^+ + 4e^- = 2H_2O$	+0.82
Fe <sup>3+</sup>	$Fe^{3+} + e^- = Fe^{2+}$	+0.77
NO <sub>3</sub> <sup>-</sup>	$2NO_3^- + 12H^+ + 10e^- = N_2 + 6H_2O$	+0.74
NO <sub>3</sub> <sup>-</sup>	$NO_3^- + 2H^+ + 2e^- = NO_2^- + H_2O$	+0.43
NO <sub>3</sub> <sup>-</sup>	$NO_3^- + 10H^+ + 8e^- = NH_4^+ + 3H_2O$	+0.36
C <sub>6</sub> H <sub>4</sub> ClCOO <sup>-</sup>	$C_6H_4ClCOO^- + H^+ + 2e^- = C_6H_5COO^- + Cl^-$	+0.26
(CH <sub>3</sub> ) <sub>2</sub> SO	$(CH_3)_2SO + 2H^+ + 2e^- = (CH_3)_2S + H_2O$	+0.23
S <sub>2</sub> O <sub>3</sub> <sup>2-</sup>	$S_2O_3^{2-} + 8H^+ + 8e^- = 2HS^- + 3H_2O$	-0.21
SO <sub>4</sub> <sup>2-</sup>	$SO_4^{2-} + 9H^+ + 8e^- = HS^- + 4H_2O$	-0.22
CO <sub>2</sub>	$CO_2 + 8H^+ + 8e^- = CH_4 + 2H_2O$	-0.24
S	$S + H^+ + 2e^- = HS^-$	-0.27



## Cálculos relacionados a la bioenergía

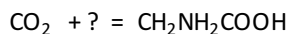
- Balancing half reactions
- Stoichiometry
- Electron and Oxygen Equivalents
- Yield
- Alkalinity/acidity



## Balaneo de Reacciones Medias

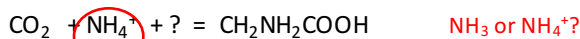
Example: half reaction for reduction of  $\text{CO}_2$  to glycine ( $\text{CH}_2\text{NH}_2\text{COOH}$ ). Carbon changes oxidation state.

1) For reduction reactions: **oxidant +  $ne^- \rightarrow$  reductant**



In reverse, this reaction is the oxidation of glycine to  $\text{CO}_2$ .

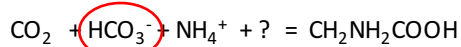
2) Balance elements other than C, H, & O, such as nitrogen.



Balance N with either  $\text{NH}_3$  or  $\text{NH}_4^+$ . Balancing with  $\text{NH}_3$  is somewhat easier to do, and it will still give the appropriate electron balance, but it will not give the correct speciation. This is because most solutions containing microbial activity have pH levels close to 7, and at these pH values,  $\text{NH}_4^+$  is the prevalent form (pKa of ammonium is 9.2).



3) Balance the carbon with  $\text{CO}_2$  and  $\text{HCO}_3^-$ . Use the negative charge on  $\text{HCO}_3^-$  to cancel the positive charge on  $\text{NH}_4^+$ .



**\*NOTE.** If the electron donor is both organic and a conjugate base (i.e., a species that can pick up a proton), then the negative charge on the conjugate base should be balanced by the negative charge on  $\text{HCO}_3^-$ .

e.g. for acetate:

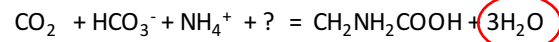


**Why is this?** When acetate or another conjugate base is added to water, it is added as a salt with a cation, such as  $\text{Na}^+$  or  $\text{K}^+$ . Degradation of acetate does not destroy its associated cation, but electroneutrality must still be maintained.

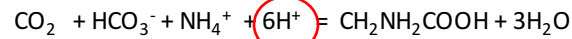
Therefore, the oxidation of a conjugate base, such as acetate, must be balanced in the half reaction by an equivalent concentration of  $\text{HCO}_3^-$ .



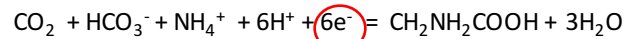
4) Balance the oxygen with H<sub>2</sub>O.



5) Balance the hydrogen with protons.



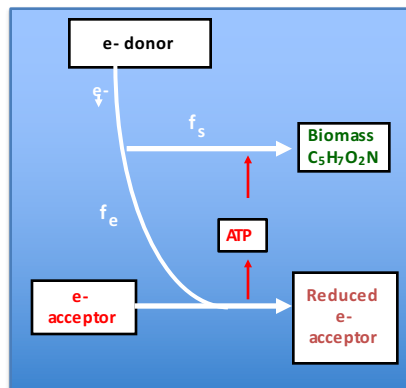
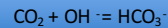
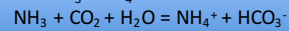
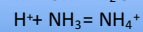
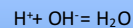
6) Add electrons as needed to give the same net charge on both sides of the equals sign.



7) Final checks:

- When adding half reactions, e<sup>-</sup> must cancel
- Correct the acid-base chemistry. Acids such as H<sup>+</sup> or CO<sub>2</sub> and bases such as NH<sub>3</sub> or OH<sup>-</sup> will not appear together on the same side of the equals sign because they neutralize one another.

Ex. Acid-base reactions:



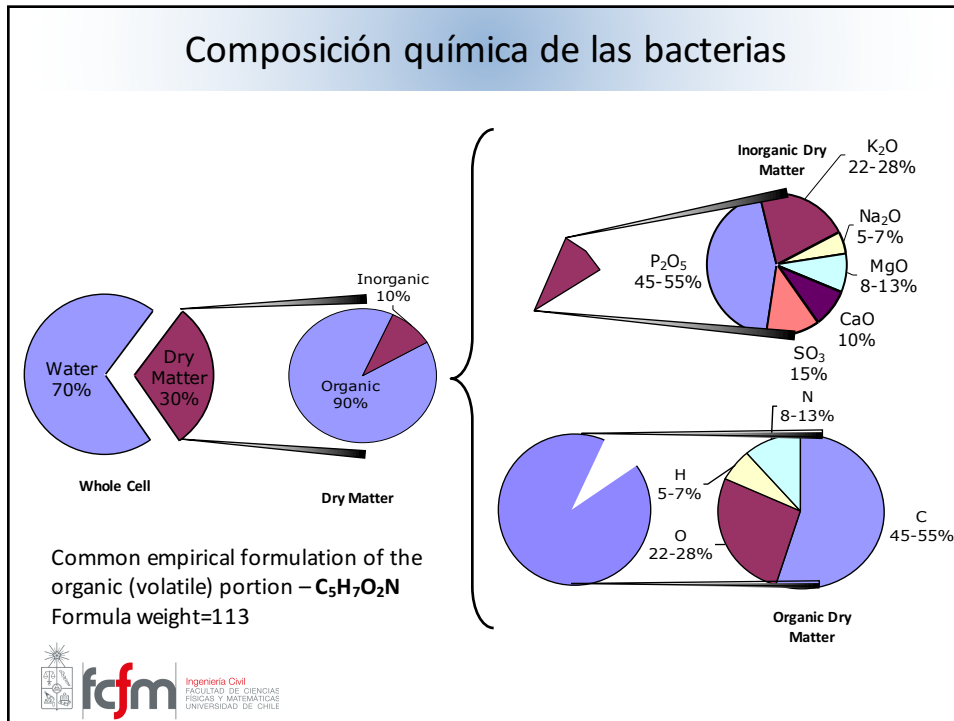
## Estequiometría de reacciones biológicas

$$f_s + f_e = 1$$

$$f_s = \frac{\text{e- equivalents of biomass formed}}{\text{electron equivalents of electron donor consumed}}$$

$$f_e = \frac{\text{e- equivalents of e- acceptor consumed}}{\text{electron equivalents of electron donor consumed}}$$

$$f_e = \frac{\text{e- equivalents of reduced e- acceptor formed}}{\text{electron equivalents of electron donor consumed}}$$



### Estequiometría de reacciones microbianas

Complete Reaction (R)     $R = R_d + f_e R_a + f_s R_c$

Electron donor half reactions (R<sub>d</sub>):

Oxidation reactions  
(See R&M Tables 2.3, 2.2)

Organic:

$$\frac{1}{e} C_a H_b O_c N_d + \frac{2a-c}{e} H_2O = \frac{a}{e} CO_2 + \frac{d}{e} NH_3 + H^+ + e^-$$

where  $e = 4a + b - 2c - 3d$

Inorganic:

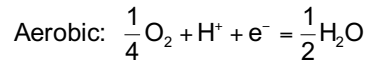
$$\frac{1}{8} NH_3 + \frac{3}{8} H_2O = \frac{1}{8} NO_3^- + \frac{9}{8} H^+ + e^- \quad \text{Ammonia oxidation}$$

$$Fe^{2+} = Fe^{3+} + e^- \quad \text{iron oxidation}$$

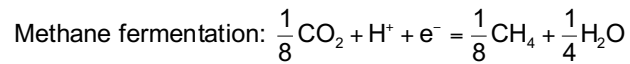
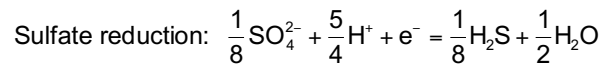
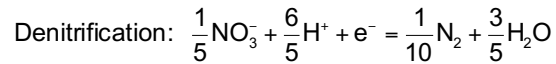
**fcfm** Ingeniería Civil  
FACULTAD DE CIENCIAS FÍSICAS Y MATEMÁTICAS  
UNIVERSIDAD DE CHILE

## Estequiometría de reacciones microbianas

### Electron acceptor half reactions ( $R_a$ ):



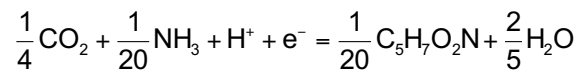
Reduction reactions  
(See R&M Tables 2.4)



## Estequiometría de reacciones microbianas

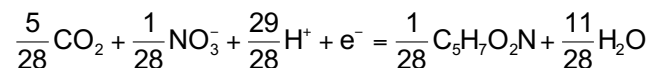
### Cell synthesis half reactions ( $R_c$ ):

Ammonia N source:

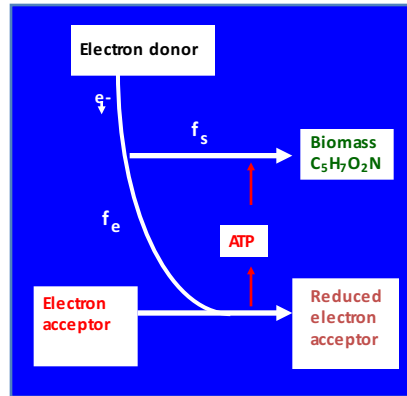


Cell growth reactions  
(See R&M Tables 2.4)

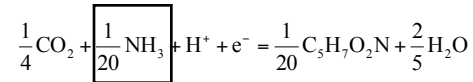
Nitrate N source:



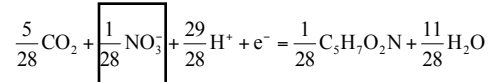
## Reacciones medias para síntesis



Cell growth using **ammonia** for N

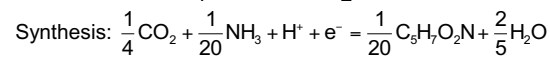
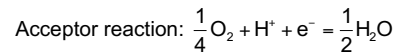
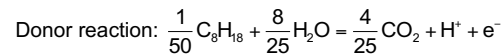


Cell growth using **nitrate** for N

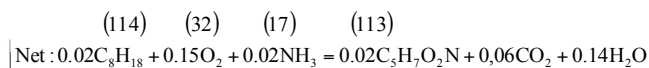
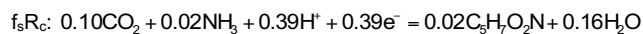
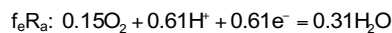
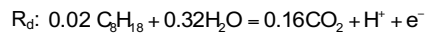


## Ejemplo: Utilización aeróbica de hidrocarburos

Hydrocarbon: octane  
Nitrogen source: ammonia



Using measured value for  $f_s$  of 0.39,  $f_e = 1 - 0.39 = 0.61$



Mass balance for the degradation of 1 kg octane:

$$\text{O}_2 \text{ required} = \frac{(0.15)(32)}{(0.02)(114)} = 2.1 \text{ kg}$$

$$\text{NH}_3 \text{ required} = \frac{(0.02)(17)}{(0.02)(114)} = 0.15 \text{ kg}$$

$$\text{Biomass produced} = \frac{(0.02)(113)}{(0.02)(114)} = 1.0 \text{ kg}$$

CHECK on mass balance:

Reactants:

Octane	1.0 kg
Ammonia	0.2 kg
O <sub>2</sub>	<u>2.1 kg</u>
	3.3 kg

Products:

CO <sub>2</sub>	1.2 kg
Cells	1.0 kg
Water	<u>1.1 kg</u>
	3.3 kg

Looks good!



## Medidas agregadas o Aggregate measures: e<sup>-</sup> eq y O<sub>2</sub> eq

An **electron equivalent** conversion factor describes an electron donor or a collection of electron donors in terms of the moles of valence electrons (equivalents) that can be removed from it.

$$\text{e- equivalents (meq)} = \text{mass (mg compound)} \div \text{e- eq conv. factor (mg compound/meq)}$$

An **oxygen equivalent** conversion factor describes an electron donor or a collection of electron donors in terms of the oxygen that is theoretically needed to oxidize it. For organic electron donors, this is the COD'/WT ratio.

**Oxygen equivalents**  
(mg COD or ThOD or  
NOD)

= **Mass**  
(mg compound)

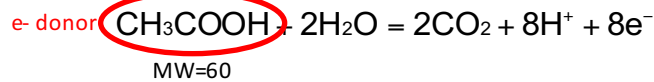
× **Oxygen equivalent  
conversion factor**  
(mg O<sub>2</sub> equivalents/ mg  
compound)

(e.g., COD'/wt ratio)





**Ejemplo: Cuál es el factor de conversión en e- eq para el acetato?**



60 grams of acetic acid surrenders 8 moles of electrons or 8 e-equivalents

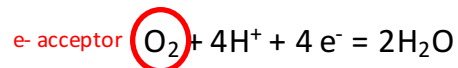
Electron equivalent conversion factor =  $60 \text{ g} / 8 \text{ eq} = 7.5 \text{ g/eq} = 7.5 \text{ mg/meq}$

The electron equivalent concentration of 100 mg/L acetic acid is  $100 \div 7.5 = 13.3 \text{ meq/L}$  or 13.3 mmoles of electrons per liter.

**Note:** If we know the concentrations of carbon, hydrogen, nitrogen and oxygen in a waste, we can compute the equivalent concentration in e-equivalents using this procedure.



**Ejemplo: Cuál es el factor de conversión en e- eq para el oxígeno?**



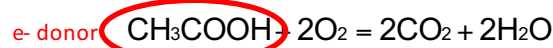
32 g of  $\text{O}_2$  accepts 4 moles of electrons, so the electron equivalent conversion factor for  $\text{O}_2$  is  $32/4 = \underline{8 \text{ g O}_2/\text{eq}}$

**8 g  $\text{O}_2$  can accept 1 mol  $\text{e}^-$   
8 g OD (COD or NOD) gives up 1 mol  $\text{e}^-$**

10 mg/L  $\text{O}_2$  accepts  $10/8 = 1.25$  mmoles of  $\text{e}^-/\text{L}$   
10 mg/L COD gives up 1.25 mmoles of  $\text{e}^-/\text{L}$



**Ejemplo: Cuál es la concentración O<sub>2</sub> eq para 100 mg/L acetato?**



$$\text{MW} = 60 \quad 2 \times 32$$

Computed O<sub>2</sub> eq conversion factor = COD'/WT = 2(32) g COD'/60 g acetate = 1.07

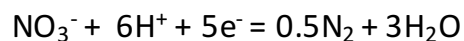
The O<sub>2</sub> eq concentration of 100 mg acetic acid /L is 100 × 1.07 = 107 mg/L.

**Note:** If we know the concentrations of carbon, hydrogen, nitrogen and oxygen in a waste, we can compute the oxygen equivalents using this procedure.



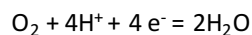
**Ejemplo: receptores de e- expresados en O<sub>2</sub> eq**

The half reaction for the reduction of nitrate to nitrogen is:



62 g of NO<sub>3</sub><sup>-</sup> picks up 5 moles of electrons, or 12.4 g NO<sub>3</sub><sup>-</sup>/mole e<sup>-</sup>

The oxygen half reaction is:



32 g of O<sub>2</sub> picks up 4 moles of electrons, or 8 g O<sub>2</sub>/mole e<sup>-</sup>

Therefore, 12.4 g NO<sub>3</sub><sup>-</sup> has the same oxidation power as 8 g O<sub>2</sub>

The oxygen equivalent conversion factor for nitrate is 8/12.4 = 0.645 g O<sub>2</sub>/g NO<sub>3</sub><sup>-</sup>.

The oxidizing power of one gram NO<sub>3</sub><sup>-</sup> is equivalent to 0.645 g O<sub>2</sub>.



## Equivalentes de O<sub>2</sub> para la célula

### COD of cells

$$\text{C}_5\text{H}_7\text{O}_2\text{N} + 5\text{O}_2 = 5\text{CO}_2 + \text{NH}_3 + 2\text{H}_2\text{O} \quad \frac{\text{COD}}{\text{WT}} = \frac{5(32)}{113} = 1.416$$

### NOD of cells

When oxidized, each mole of C<sub>5</sub>H<sub>7</sub>O<sub>2</sub>N yields 1 mole NH<sub>3</sub>. When the NH<sub>3</sub> is oxidized:



### ThOD of cells (COD + NOD)

$$\text{C}_5\text{H}_7\text{O}_2\text{N} + 7\text{O}_2 = 5\text{CO}_2 + \text{HNO}_3 + 3\text{H}_2\text{O} \quad \frac{\text{ThOD}}{\text{WT}} = \frac{7(32)}{113} = 1.98$$



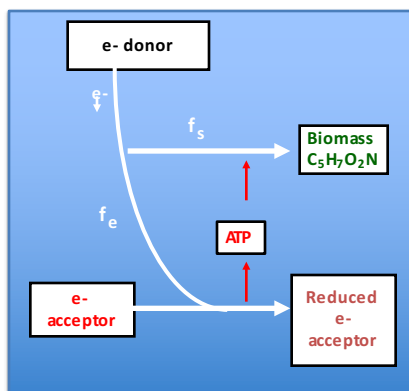
### Common conversion factors for electron equivalents and oxygen equivalents

Compound	Electron equivalent conversion factor	Oxygen equivalent conversion factor
<b>Electron donors</b>		
methane	2.0 g CH <sub>4</sub> /eq	4.0 g COD/g CH <sub>4</sub>
carbohydrate	7.5 g carbohydrate/eq	1.067 g COD /g carbohydrate
protein	5.333 g protein/eq	1.50 g COD /g protein
grease (fat)	2.778 g grease/eq	2.88 g COD /g grease
sewage organics	4.02 g sewage organic/eq	1.99 g COD /g sewage organic
ammonium (to nitrate)	2.254 g NH <sub>4</sub> <sup>+</sup> /eq	3.55 g NOD /g NH <sub>4</sub> <sup>+</sup>
	1.75 g NH <sub>4</sub> <sup>+</sup> as N/eq	4.57 g NOD /g NH <sub>4</sub> <sup>+</sup> as N
ammonium (to nitrite)	3.0 g NH <sub>4</sub> <sup>+</sup> /eq	2.667 g NOD/g NH <sub>4</sub> <sup>+</sup>
nitrite (to nitrate)	23 g NO <sub>2</sub> <sup>-</sup> /eq	0.36 g NOD /g NO <sub>2</sub> <sup>-</sup>
	7 g NO <sub>2</sub> <sup>-</sup> as N/eq	1.14 g NOD/g NO <sub>2</sub> <sup>-</sup> as N
S (to sulfate)	5.333 g S/eq	1.50 g Sulfur OD /g S
H <sub>2</sub> (to H <sup>+</sup> )	1.0 g H <sub>2</sub> /eq	8.0 g Hydrogen OD/g H <sub>2</sub>
<b>Biomass (C<sub>5</sub>H<sub>7</sub>O<sub>2</sub>N)</b>		
N source: NH <sub>4</sub> <sup>+</sup>	5.65 g biomass/eq	1.42 g COD /g biomass
N source: nitrate	4.04 g biomass /eq	1.98 g ThOD/g biomass
<b>Electron acceptors</b>		
oxygen (to water)	8.0 g O <sub>2</sub> /eq	1.0 g O <sub>2</sub> /g O <sub>2</sub>
nitrate (to nitrogen)	12.4 g NO <sub>3</sub> <sup>-</sup> /eq	0.645 g O <sub>2</sub> /g NO <sub>3</sub> <sup>-</sup>
	2.8 g NO <sub>3</sub> <sup>-</sup> as N/eq	2.857 g O <sub>2</sub> /g NO <sub>3</sub> <sup>-</sup> as N
sulfate (to H <sub>2</sub> S)	12.0 g SO <sub>4</sub> <sup>2-</sup> /eq	0.667 g O <sub>2</sub> /g SO <sub>4</sub> <sup>2-</sup>
	4.0 g SO <sub>4</sub> <sup>2-</sup> as S/eq	2.0 g O <sub>2</sub> /g SO <sub>4</sub> <sup>2-</sup> as S
CO <sub>2</sub> (to methane)	5.5 g CO <sub>2</sub> /eq	1.45 g O <sub>2</sub> /g CO <sub>2</sub>
	1.5 g CO <sub>2</sub> as C/eq	5.33 g O <sub>2</sub> /g CO <sub>2</sub> as C
Cr <sub>2</sub> O <sub>7</sub> <sup>2-</sup> (to Cr <sup>3+</sup> ) (oxidant in COD test)	36 g Cr <sub>2</sub> O <sub>7</sub> <sup>2-</sup> /eq	0.222 g O <sub>2</sub> /g Cr <sub>2</sub> O <sub>7</sub> <sup>2-</sup>
<b>Reduced electron acceptors</b>		
nitrogen (from nitrate)	2.8 g N <sub>2</sub> /eq	2.857 g OD/g N <sub>2</sub>
	2.24 L N <sub>2</sub> /eq at STP	3.571 g OD/L N <sub>2</sub> at STP
H <sub>2</sub> S (from sulfate)	4.25 g H <sub>2</sub> S/eq	1.88 g OD/g H <sub>2</sub> S
methane (from CO <sub>2</sub> )	2.0 g CH <sub>4</sub> /eq	4.0 g COD/g CH <sub>4</sub>
	2.8 L CH <sub>4</sub> /eq at STP	2.857 g COD/L CH <sub>4</sub> at STP
	3.159 L CH <sub>4</sub> /eq at 35°C	2.532 g COD/L CH <sub>4</sub> at 35°C

= 8  
g OD / eq



## Conversión a equivalentes de e<sup>-</sup> y O<sub>2</sub>



Conversion to electron equivalents  
Divide each mass by appropriate electron equivalent conversion factor

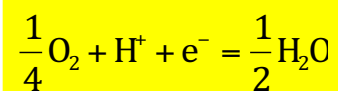
Conversion to oxygen equivalents  
Multiply each mass by appropriate oxygen equivalent conversion factor

## Conversión a equivalentes de e<sup>-</sup> y O<sub>2</sub>

### Electron equivalent balance

e- removed from e- donor =  
e- in biomass + e- in reduced e- acceptor.

e- equivalents in reduced e- acceptor =  
e- equivalents of e- acceptor consumed.



÷ 8 gOD/eq

× 8 gOD/eq

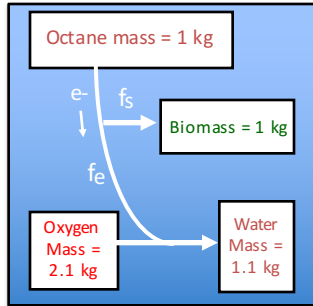
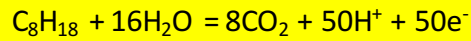
### Oxygen equivalent balance:

O<sub>2</sub> eq of e- donor consumed = O<sub>2</sub> eq in  
biomass + O<sub>2</sub> eq in reduced e- acceptor.

O<sub>2</sub> equivalents in reduced e- acceptor =  
O<sub>2</sub> equivalents of e- acceptor consumed.

Ejemplo: Cómo se balancean los equivalentes iniciales y finales para la degradación biológica de 1 kg de octano en batch?

Conversion to e- equivalents



Divide each mass by appropriate electron equivalent conversion factor:

Octane:  $114/50 = 2.28 \text{ g/eq}$   
 Biomass:  $5.65 \text{ g VSS/eq}$   
 Oxygen:  $8 \text{ g/eq}$

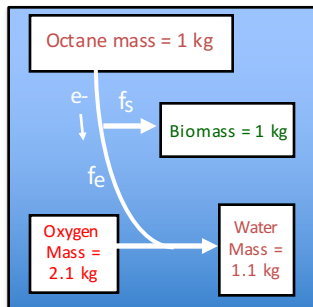
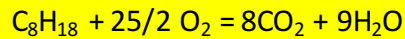
Consumed:  
 Octane  $e^- \text{ eq} = 1/2.28 = 0.44 \text{ kmoles } e^-$

Synthesis + Energy:  
 Biomass  $e^- \text{ eq} = 1/5.65 = 0.18 \text{ kmoles } e^-$   
 $O_2 e^- \text{ equiv} = 2.1/8 = 0.26 \text{ kmoles } e^-$



Ejemplo: Cómo se balancean los equivalentes iniciales y finales para la degradación biológica de 1 kg de octano en batch?

Conversion to oxygen equivalents



[CO<sub>2</sub> is the missing 1 kg of product]

Multiply each mass by appropriate oxygen equivalent conversion factor

Octane:  $(25/2 \times 32)/114 = 3.5 \text{ g OD/g octane}$   
 Biomass:  $1.42 \text{ g OD/g VSS}$   
 Oxygen:  $1 \text{ g OD/g } O_2$

Consumed:  
 Octane COD =  $1 \times 3.5 = 3.5 \text{ kg COD}$

Synthesis + Energy:  
 Biomass COD =  $1 \times 1.42 = 1.42 \text{ kg COD}$   
 Oxygen  $O_2 \text{ equiv} = 2.1 \text{ kg } O_2$

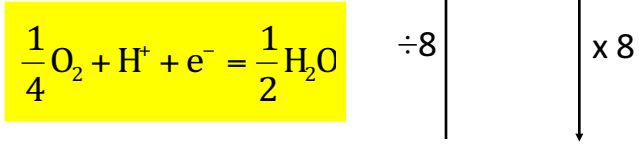


### Conversión entre equivalentes de e<sup>-</sup> y O<sub>2</sub>

Electron equivalent balance

Consumed:  
 Octane e<sup>-</sup> eq = 1/2.28 = **0.44 kmoles e<sup>-</sup>**

Synthesis + Energy:  
 Biomass e<sup>-</sup> eq = 1/5.65 = **0.18 kmoles e<sup>-</sup>**  
 O<sub>2</sub> e<sup>-</sup> equiv = 2.1/8 = **0.26 kmoles e<sup>-</sup>**



Oxygen equivalent balance:

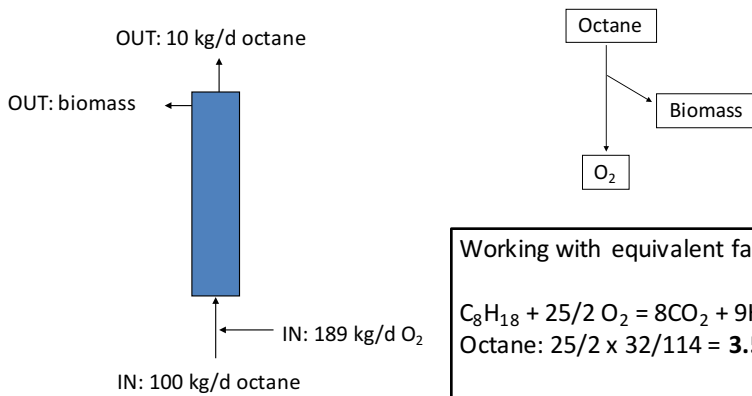
Consumed:  
 Octane COD = 1 x 3.5 = **3.5 kg COD**

Synthesis + Energy:  
 Biomass COD = 1 x 1.42 = **1.42 kg COD**  
 Oxygen O<sub>2</sub> equiv = **2.1 kg O<sub>2</sub>**



### Ejemplo: degradación continua de octano en un bioreactor

The high rate bioreactor shown below removes 90% of 100 kg/d octane and uses 189 kg/d O<sub>2</sub>. What is the biomass production rate?



Working with equivalent factors:

$C_8H_{18} + 25/2 O_2 = 8CO_2 + 9H_2O$   
 Octane:  $25/2 \times 32/114 = \mathbf{3.5 \text{ kg COD/kg}}$

$C_5H_7 O_2 N + 5O_2 = 5CO_2 + NH_3 + 2H_2O$   
 Biomass:  $5 \times 32/114 = \mathbf{1.42 \text{ kg COD/kg}}$



Solución usando  $O_2$  eq:

$O_2$  Conversion Factors:

Octane: 3.5 kg COD/kg

Biomass: 1.42 kg COD/kg

OUT: 10 kg octane x 3.5 = 35 kg/d COD

OUT:  
How much  
biomass?



189 kg/d  $O_2$

IN: 100 kg octane x 3.5 = 350 kg/d COD

COD consumed = 350 - 35 = 315 kg/d

$O_2$  equivalents for energy = 189 kg/d  $O_2$

$O_2$  equivalents for synthesis = 315 - 189  
= 126 kg/d biomass as COD

Biomass produced =  $126 \div 1.42 = 89$  kg/d

$$f_e = 189/315 = 0.60$$

$$f_s = 126/315 = 0.40$$



## Yield (Y)

$$f_s = \frac{\text{e- equivalents of biomass formed}}{\text{electron equivalents of electron donor consumed}}$$



$$Y = \frac{\text{Biomass produced}}{\text{Substrate consumed}}$$

[g VSS/ g COD]

Why VSS?

- Y can be measured and is directly related to  $f_s$ .
- Y can be changed it into  $f_s$  by converting both the numerator and the denominator into electron equivalents (or into  $O_2$  equivalents, whichever is easier).



**Ejemplo:** Given  $Y = 0.49 \text{ g vss/g COD}$ , ammonia N source. What is  $f_s$ ?

Solution using **O<sub>2</sub> equivalents:**

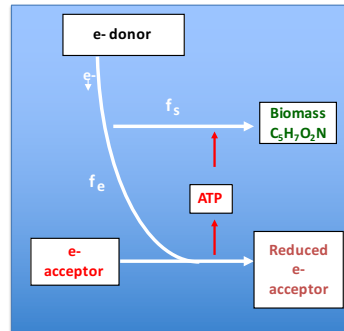
$$f_s = 0.49 \text{ g vss/g COD} \times \underline{1.42 \text{ g COD/g vss}} = 0.70$$

Solution using **electron equivalents:**

$$f_s = 0.49 \text{ g vss/g COD} \times 8 \text{ g COD/eq} \div \underline{5.65 \text{ g VS/eq}} = 0.70$$

Same result using both approaches!

How much is  $f_e$ ?



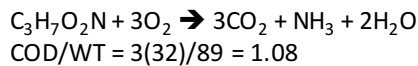
### Ejemplo de estequiometría

A meat packing waste with the empirical formula:  $C_3H_7O_2N$  (M.W. = 89). Determine the oxygen required per gram of waste for aerobic treatment.



[Klaucans et al., 2018. \(10.4028/www.scientific.net/KEM.762.61\)](https://doi.org/10.4028/www.scientific.net/KEM.762.61)

Parameter	See food processing wastewaters [mg/L]	Meat processing wastewaters [mg/L]	Restaurant wastewaters [mg/L]	Typical municipal wastewaters [mg/L]
Total COD	8 000–18 700	9 600–12 900	1250–4500	210–740
Total BOD	1000–72 000	2 500–8 000	820–3000	150–350
Total suspended solids (TSS)	500–2000	790–3 350	220–2700	120–450
Total Nitrogen (N <sub>tot</sub> )	200–300	230–260	–	20–80
Total Phosphorus (P <sub>tot</sub> )	–	30–50	–	6–23
FOG [mg/L]	250–5000	100–2000	140–4100	–



Will aerobic biological treatment of this wastewater require 1.08 g O<sub>2</sub>/g waste?

If Y for aerobic growth is 0.32 g vss/g COD  
 $f_s = 0.32 \times 1.42 = 0.45$  and  $f_e = 1 - 0.45 = 0.55$

so the amount of oxygen required is  $0.55 \times 1.08 = 0.59 \text{ g O}_2/\text{g}$ .



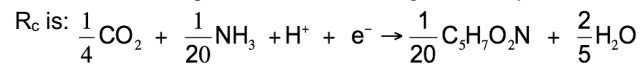
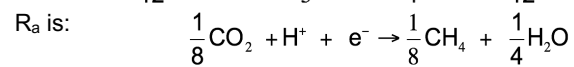
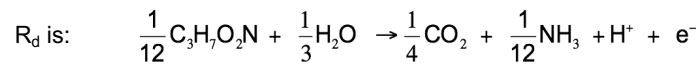


## Ejemplo de estequiometría: Anaerobio

Determine the nutrient requirements and methane production per gram of waste for anaerobic treatment.

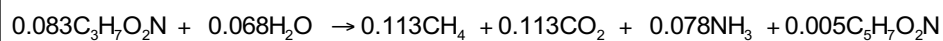
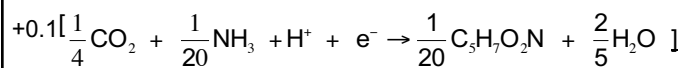
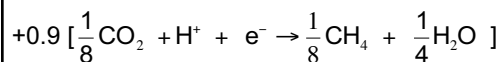
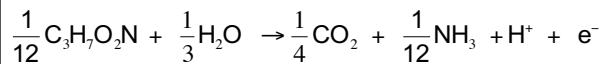
Assuming an anaerobic yield of 0.07 g vss/g COD, then  $f_s = 0.07 \times 1.42 = 0.1$ .

First, we write the half reaction for oxidation of the electron donor (for now we'll ignore acid-base reactions):  $C_3H_7O_2N + 4H_2O \rightarrow 3CO_2 + NH_3 + 12H^+ + 12e^-$



## Ejemplo de estequiometría: Anaerobio

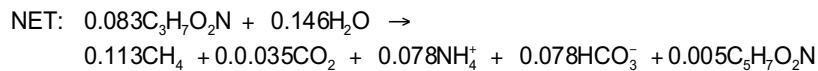
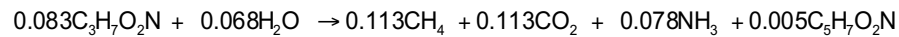
Weighting  $R_a$  by  $f_e$  and  $R_c$  by  $f_s$  and putting them all together:



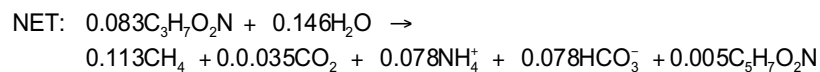
## Ejemplo de estequiometría: Anaerobio

We do not need to add nitrogen.

In fact, the reaction actually produces nitrogen as ammonia, but... if we want to know how much CO<sub>2</sub> is produced, we will have to correct for the fact that some of it will be neutralized by the NH<sub>3</sub> that is produced:



## Ejemplo de estequiometría: Anaerobio



With the balanced acid-base reaction, we can calculate the % methane in the biogas:

$$\% \text{CH}_4 = 0.113 / (0.113 + 0.035) \times 100 = 76\%$$

(so there is 24% CO<sub>2</sub>)

Methane production @ STP

$$(0.113)(22.4 \text{ L methane/mole}) \div (0.083)(89) = 0.342 \text{ L/g waste}$$

This is for STP conditions, the temperature is 0°C.

Do you know how to adjust for different temperatures?



## Ejemplo de estequiometría: Anaerobio

### What is the phosphorus requirement of the cells?

Suppose this wastewater has a biodegradable COD ( $BOD_L$ ) of 10 g/L and no P is present in the waste? The COD removal efficiency is 100%, and P is 2% (by weight) of the vss.

P requirement =

$$\frac{10 \text{ g COD}}{\text{L}} \times \frac{\text{mol e}^-}{8 \text{ g COD}} \times \frac{(0.005)(113 \text{ g vss})}{\text{mol e}^-} \times \frac{0.02 \text{ g P}}{\text{g vss}} =$$

$$\frac{0.014 \text{ g P}}{\text{L}}$$



## Ejemplo de estequiometría: Anaerobio

How many liters of methane will be produced per liter of waste if the treatment efficiency is 100%?

$$\frac{\text{Liters methane}}{\text{Liter waste}} = \frac{10 \text{ g COD}}{\text{L}} \times \frac{\text{mol e}^-}{8 \text{ g COD}} \times \frac{0.113 \text{ mol CH}_4}{\text{mol e}^-} \times \frac{22.4 \text{ L}}{\text{mol CH}_4} = \frac{3.15 \text{ liters}}{\text{liter of waste}}$$

NOTE: problem could just as easily be solved using the oxygen equivalent conversion factor for methane:

$$\frac{\text{Liters methane}}{\text{Liter waste}} = \frac{10 \text{ g COD}}{\text{L}} \times \frac{0.9 \text{ g COD to CH}_4}{\text{g COD}} \times \frac{\text{L CH}_4}{2.857 \text{ g COD}} = \frac{3.15 \text{ liters}}{\text{liter of waste}}$$

This is for STP conditions, the temperature is 0°C.

Do you know how to adjust for different temperatures?



## Energía libre y Yield

### Why do some microorganisms have a lower yield than others?

Microorganisms “prefer” to convert all their substrate into biomass ( $f_s = 1.0$ ), but some substrate must be burned to give energy for synthesis.

When energy reactions yield very little energy per equivalent, most of the electrons must be used to produce energy for cell synthesis ( $f_e$  must be large). For these reactions,  $f_s$  and yield will be small.

Other energy reactions generate considerable energy per equivalent. Fewer equivalents can generate sufficient energy for cell synthesis ( $f_e$  can be small). For these reactions,  $f_s$  and yield will be large.



## Alcalinidad

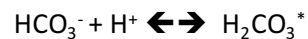
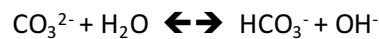
Alkalinity: The ability to neutralize strong acids

the cumulative proton concentration taken up by basic species when a solution is titrated to the  $\text{CO}_2$  equiv pt (around pH 4.3-4.7):

$$\text{Alkalinity} = -(\text{H}^+) + (\text{HCO}_3^-) + 2(\text{CO}_3^{2-}) + (\text{NH}_3) + (\text{HS}^-) + (\text{OH}^-)$$

### Example: Dissolve $\text{CaCO}_3$ in water

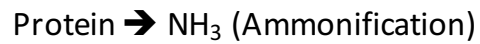
$\text{CO}_3^{2-}$  equilibrates with  $\text{HCO}_3^-$  and  $\text{H}_2\text{CO}_3^*$  according to:



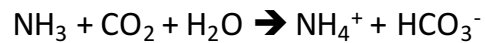
## La alcalinidad cambia de forma

### Biological Examples

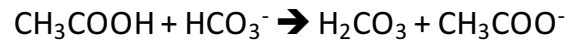
1. Bacteria release  $\text{NH}_3$  from protein:



2. Ammonia reacts with carbon dioxide



3. Volatile fatty acids can react with  $\text{HCO}_3^-$ :

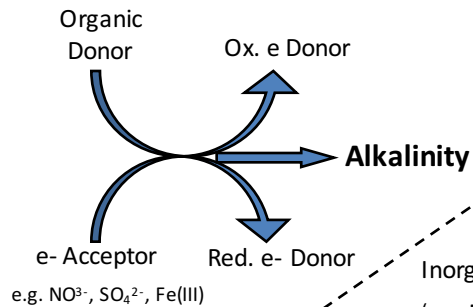


Where has the alkalinity gone?



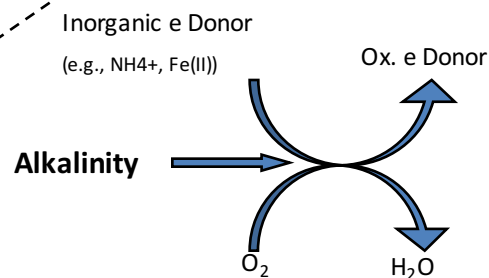
## Procesos microbianos pueden producir o consumir alcalinidad

### *Typical Anaerobic Process*



Sometimes!

### *Typical Aerobic Process*



## Fuentes de buffer alcalino

Alkaline buffer (salt/base)	Dissolution and Neutralization reactions	How many kg of the buffer are equivalent to one kmol of alkalinity?	Comments	1995 Cost(\$ per kmol Alkalinity)
CaCO <sub>3</sub>	CaCO <sub>3</sub> + 2H <sup>+</sup> = Ca <sup>2+</sup> + H <sub>2</sub> CO <sub>3</sub> CaCO <sub>3</sub> + H <sub>2</sub> O + CO <sub>2</sub> = Ca <sup>2+</sup> + 2HCO <sub>3</sub> <sup>-</sup>	100 g of CaCO <sub>3</sub> neutralizes 2 moles of strong acid, 100 g of CaCO <sub>3</sub> reacts with CO <sub>2</sub> to make 2 moles of HCO <sub>3</sub> <sup>-</sup> . We have 100 + 2 = 50 kg CaCO <sub>3</sub> per kmol of alkalinity.	Poor solubility restricts alkalinity to 1400-1500 mg/L as CaCO <sub>3</sub>	Not available (cheap)
Na <sub>2</sub> CO <sub>3</sub>	Na <sub>2</sub> CO <sub>3</sub> + 2H <sup>+</sup> = 2Na <sup>+</sup> + H <sub>2</sub> CO <sub>3</sub> Na <sub>2</sub> CO <sub>3</sub> + H <sub>2</sub> O + CO <sub>2</sub> = 2Na <sup>+</sup> + 2HCO <sub>3</sub> <sup>-</sup>	106 + 2 = 53 kg	Na is inhibitory at 3,500 mg/L. Na deflocculates soil.	11.55
K <sub>2</sub> CO <sub>3</sub>	Like Na <sub>2</sub> CO <sub>3</sub>	136 + 2 = 68 kg	K is inhibitory at > 2,500 mg/L.	Not available
(NH <sub>4</sub> ) <sub>2</sub> CO <sub>3</sub>	(NH <sub>4</sub> ) <sub>2</sub> CO <sub>3</sub> = 2NH <sub>4</sub> <sup>+</sup> + CO <sub>3</sub> <sup>2-</sup> CO <sub>3</sub> <sup>2-</sup> + 2H <sup>+</sup> = H <sub>2</sub> CO <sub>3</sub>	96 + 2 = 48 kg		Not available
CaO (lime)	CaO + 2H <sub>2</sub> O = Ca(OH) <sub>2</sub> Ca(OH) <sub>2</sub> + 2H <sup>+</sup> = Ca <sup>2+</sup> + 2H <sub>2</sub> O Ca(OH) <sub>2</sub> + 2CO <sub>2</sub> = Ca <sup>2+</sup> + 2HCO <sub>3</sub> <sup>-</sup>	56 + 2 = 28 kg	Can cause severe scaling @ pH>6.8. Can create a vacuum in a closed system.	3.74
MgO	Like CaO	40 + 2 = 20 kg	Low solubility reduces chance of pH overshoot.	7.71
NaHCO <sub>3</sub>	NaHCO <sub>3</sub> + H <sub>2</sub> O = Na <sup>+</sup> + HCO <sub>3</sub> <sup>-</sup> HCO <sub>3</sub> <sup>-</sup> + H <sup>+</sup> = H <sub>2</sub> CO <sub>3</sub>	84 kg	Exactly the right form, but expensive.	36.89
NaOH	NaOH + H <sup>+</sup> = Na <sup>+</sup> + H <sub>2</sub> O NaOH + CO <sub>2</sub> = Na <sup>+</sup> + HCO <sub>3</sub> <sup>-</sup>	40 kg	Can create a vacuum in a closed system	35.20
KOH	Like NaOH	56 kg	Can create a vacuum in a closed system	Not available
NH <sub>3</sub>	NH <sub>3</sub> + H <sup>+</sup> = NH <sub>4</sub> <sup>+</sup> NH <sub>3</sub> + CO <sub>2</sub> + H <sub>2</sub> O = NH <sub>4</sub> <sup>+</sup> + HCO <sub>3</sub> <sup>-</sup>	17 kg	Can be toxic. Released as protein degrades.	Not available



## Acidity

Acidity: the cumulative hydroxide concentration taken up by acidic species when a solution is titrated to the CO<sub>3</sub><sup>2-</sup> equiv. pt.:

$$\text{Acidity} = (\text{H}^+) + (\text{HCO}_3^-) + 2(\text{H}_2\text{CO}_3^*) + (\text{NH}_4^+) - (\text{OH}^-)$$

*Note that HCO<sub>3</sub><sup>-</sup> contributes to alkalinity and acidity*

The two major sources of acidity in biological systems are:



In covered reactors, CO<sub>2</sub> accumulates in the in gas phase, causing H<sub>2</sub>CO<sub>3</sub><sup>\*</sup> to accumulate and pH to drop.

HCO<sub>3</sub><sup>-</sup> buffer must be added to decrease pH drop.

